## MATH M11: COLLEGE ALGEBRA FOR THE LIBERAL ARTS

## Originator

Phillip Abramoff

## Co-Contributor(s)

## Name(s)

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## College

Moorpark College

## Attach Support Documentation (as needed)

MATH M11_state approval letter_CCC000608544.pdf
Discipline (CB01A)
MATH - Mathematics
Course Number (CB01B)
M11
Course Title (CB02)
College Algebra for the Liberal Arts

## Banner/Short Title

College Algebra for Lib Arts

## Credit Type

Credit

## Honors

No

## Start Term

Fall 2020

## Catalog Course Description

Covers theory of functions including operations on functions, graphs, domain and range, and evaluation. Includes types of functions such as linear, quadratic, polynomial, rational, exponential and logarithmic functions. Analyzes graphs including curve sketching, intercepts, transformations, vertices and asymptotes. Covers linear and non-linear inequalities, solving exponential and logarithmic equations and complex numbers.

## Additional Catalog Notes

Course is intended primarily as a prerequisite for students taking Business Calculus, and for students requiring college algebra content for non-STEM majors.
Credit Course Limitation: No more than 4 units may be awarded for students who complete both MATH M05 and MATH M11.
Taxonomy of Programs (TOP) Code (CBO3)
1701.00 - Mathematics, General

Course Credit Status (CB04)
D (Credit - Degree Applicable)
Course Transfer Status (CB05) (select one only)
A (Transferable to both UC and CSU)

## Course Basic Skills Status (CB08)

N - The Course is Not a Basic Skills Course
SAM Priority Code (CB09)
E - Non-Occupational

Course Cooperative Work Experience Education Status (CB10)
N - Is Not Part of a Cooperative Work Experience Education Program
Course Classification Status (CB11)
Y - Credit Course
Educational Assistance Class Instruction (Approved Special Class) (CB13)
N - The Course is Not an Approved Special Class
Course Prior to Transfer Level (CB21)
Y - Not Applicable
Course Noncredit Category (CB22)
Y - Credit Course
Funding Agency Category (CB23)
Y - Not Applicable (Funding Not Used)
Course Program Status (CB24)
1 - Program Applicable
General Education Status (CB25)
B - Satisfies Math/Quantitative Reasoning req (CSUGE-B B4, IGETC 2, or 4-yr)
Support Course Status (CB26)
N - Course is not a support course
Field trips
Will not be required
Grading method
Letter Graded
Alternate grading methods
Pass/No Pass Grading
Does this course require an instructional materials fee?
No
Repeatable for Credit
No
Is this course part of a family?
No

## Units and Hours

Carnegie Unit Override
No
In-Class
Lecture
Minimum Contact/In-Class Lecture Hours
52.5

Maximum Contact/In-Class Lecture Hours
52.5

Activity
Laboratory

## Total in-Class

Total in-Class
Total Minimum Contact/In-Class Hours 52.5

Total Maximum Contact/In-Class Hours 52.5

## Outside-of-Class

Internship/Cooperative Work Experience
Paid
Unpaid
Total Outside-of-Class
Total Outside-of-Class
Minimum Outside-of-Class Hours
105
Maximum Outside-of-Class Hours
105
Total Student Learning
Total Student Learning
Total Minimum Student Learning Hours
157.5

Total Maximum Student Learning Hours
157.5

Minimum Units (CB07)
3
Maximum Units (CB06)
3

## Prerequisites

MATH M03 or MATH M03B or High School Algebra II or placement as determined by college's multiple measures assessment process.

## Entrance Skills

Entrance Skills
MATH M03 or MATH M03B or High School Algebra II or placement as determined by college's multiple measures assessment process.

## Requisite Justification

Requisite Type
Prerequisite
Requisite
MATH M03 or MATH M03B
Requisite Description
Other (specify)

## Specify Other Requisite Description

or High School Algebra II or placement as determined by college's multiple measures assessment process.

## Level of Scrutiny/Justification

Required by 4 year institution

## Student Learning Outcomes (CSLOs)

| Upon satisfactory completion of the course, students will be able to: |  |  |  |
| :--- | :--- | :---: | :---: |
| 1 | solve a linear system of two variables, and identify whether the system is independent, dependent or inconsistent. |  |  |
| 2 | solve an application problem requiring the use of logarithms to solve an exponential equation. |  |  |
| 3 | successfully determine all the roots of a polynomial function by employing the Rational Root Theorem, the Remainder <br> Theorem, and synthetic division. |  |  |
| 4 | successfully identify the transformations of a basic function and graph the function on a Cartesian plane. |  |  |

## Course Objectives

## Upon satisfactory completion of the course, students will be able to:

$1 \quad$ state and apply the definition of a function and identify whether a relation is a function.
2 determine the domain and range of a function, and evaluate the function at a numerical or algebraic value.
3 perform basic operations on functions, including addition, subtraction, multiplication, division and composition of functions, and determining the inverse of a one-to-one function.
4 identify transformations of functions, in comparison to basic function graphs, including shape change, reflection, horizontal and vertical shift, and sketch graph.
5
identify features of the graph of a function, including intercepts, vertices, maximum and minimum values, asymptotes and symmetry.
6 solve equations and determine roots of various functions, including linear, quadratic, polynomial and rational functions.

7 solve inequalities, including linear, quadratic, polynomial and rational inequalities, stating answer in set notation or interval notation.
8
9 sketch the graph of a polynomial of degree three or higher, using the roots of the polynomial and its factored form. sketch the graph of a rational function, using the roots, asymptotes and intervals where function is positive or negative.
sketch the graph of basic exponential and logarithmic graphs.
12 use properties of logarithms to simplify logarithmic expressions.
13 solve exponential equations using properties of exponents, logarithms, and the change of base formula to find numerical solutions to equations that may or may not have a common base on both sides of an equation.
solve logarithmic equations using properties of logarithms.
use the techniques of solving exponential and logarithmic equations to solve application problems in biology, economics or other scientific fields.
solve systems of linear equations involving two variables, using substitution or elimination, and stating whether system is independent, dependent or inconsistent.
17 solve systems of linear equations involving three variables, using substitution or elimination, and stating whether system is independent, dependent or inconsistent.
perform basic operations on complex numbers, including addition, subtraction, multiplication, division and determining the conjugate of a complex number.
19 determine all roots of a quadratic equation by using factoring, completing the square and the quadratic formula, including complex roots if they occur.

## Course Content

## Lecture/Course Content

## 10\% A. Equations and Inequalities

1. Solving linear equations
2. Solving quadratic equations
3. Solving polynomial equations
4. Solving linear inequalities
5. Solving quadratic and other polynomial inequalities

10\% B. Theory of Functions

1. Definition of a relation and a function
2. Determine whether a relation is a function and determine domain and range
3. Evaluating a function at a value
4. Addition, subtraction, multiplication, division and composition of functions
5. One-to-one functions and inverses

## 20\% C. Graphs of Functions

1. Graphs of basic functions
2. Transformations, shifts, shape change, reflection and vertices
3. Graph symmetry
4. Features of the graph of a parabola
5. Graphs of polynomials including roots and intercepts
6. Graphs of rational functions, including roots and asymptotes

20\% D. Polynomial and Rational Functions

1. Quadratic functions, completing the square and the quadratic formula
2. Roots of polynomial functions
3. Synthetic division, Remainder Theorem and Rational Root Theorem
4. Sketching graph of polynomial function using roots
5. Rational functions
6. Roots of rational functions
7. Horizontal and vertical asymptotes
8. Sketching graph of rational function
9. Solving polynomial inequalities
10. Solving rational inequalities
11. Complex numbers
12. Basic operations on complex numbers and conjugate
13. Complex roots of quadratic and polynomial functions

25\% E. Exponential and Logarithmic Functions

1. Graph of an exponential functions
2. Solving exponential equations in same base
3. The natural exponent "e"
4. The definition of logarithm
5. Properties of logarithms and simplifying logarithmic expressions
6. Graph of a logarithmic function
7. Solving logarithmic equations
8. Solving exponential equations using logarithms
9. Applications of logarithms in economics and sciences
10. Compound and continuous interest (optional)
11. Exponential growth and decay (optional)

## $10 \%$ F. Systems of Equations

1. Solving linear systems in two variable by graphing, substitution or elimination
2. Independent, dependent and inconsistent systems of equations
3. Solving linear systems of equations in three variable by Gaussian elimination
4. Solving non-linear systems of equations in two variables (optional)
5. Solving linear inequalities in two variables (optional)

## Laboratory or Activity Content

Not applicable

## Methods of Evaluation

Which of these methods will students use to demonstrate proficiency in the subject matter of this course? (Check all that apply):
Problem solving exercises
Methods of Evaluation may include, but are not limited to, the following typical classroom assessment techniques/required assignments (check as many as are deemed appropriate):
Essay exams
Objective exams
Other (specify)
Problem-solving exams
Reports/papers

## Other

Graded homework assignments which are used to evaluate student progress in practicing and mastering computational skills In class quizzes and/or graded work in class whereby students demonstrate step-by-step solutions to problems, and demonstrate knowledge of abstract concepts by interpreting and explaining the meaning of answers

## Instructional Methodology

## Specify the methods of instruction that may be employed in this course

Distance Education
Lecture
Other (specify)

## Specify other method of instruction

Provide additional practice problems to develop proper problem solving skills and understanding of abstract topics
Discuss applications of mathematical concepts, such as using biological or financial models to illustrate use of logarithms to solve exponential functions which occur in ordinary life

## Describe specific examples of the methods the instructor will use:

1. Use of whiteboard or overhead projector to demonstrate solutions to calculations, such as identifying zeros, roots, domains and asymptotes of polynomial or rational functions.
2. Classroom discussion, with student response, such as discussing the meaning of the definition of function.
3. In class group activities, such as guided practice on solving various types of equations such as polynomial, exponential or logarithmic equations for numerical solutions.

## Representative Course Assignments

## Writing Assignments

1. stating the answer to a mathematical problem in any of various forms, such as stating the answer to an inequality in interval notation or set builder notation.
2. writing the interpretation of an answer to a mathematical problem, such as the meaning of the solution to an exponential equation with proper labeling of units.
3. writing a short answer explaining the meaning of mathematical terms, such as the difference between relation, function, and one-to-one function.

## Critical Thinking Assignments

1. compare and contrast methods of solving a mathematical problem, such as determining whether to factor, complete the square or apply the quadratic formula to solve a quadratic equation.
2. describe and analyze the steps in solving a problem, such as identifying and labeling the several steps in solving a linear system in three variables, using Gaussian elimination.
3. interpret and describe the meaning of the solution to a mathematical application problem, such as an answer representing either time, an amount of money, or an interest rate in a compound interest application problem solved by using logarithms.

## Reading Assignments

1. Reading concepts from the textbook, such as the description of the differences between a relation, function and one-to-one function.
2. Reading instructor created materials, such as a prepared handout describing the meaning of intercepts, roots, turning points and asymptotes in the graphs of functions.
3. Reading resource materials from the library or online concerning real-life applications of exponents and logarithms in economics and sciences.

## Skills Demonstrations

1. Demonstration of computational skills such as factoring or simplifying mathematical expressions.
2. Demonstrating the understanding of the meaning of an answer, such as interpreting the meaning of an ordered-pair answer in an application problem.
3. Demonstration of the proper use of a calculator in finding the numerical solution to an application problem involving exponents or logarithms, and expressing answer with proper numerical rounding and proper label

## Outside Assignments

## Representative Outside Assignments

1. individual or group assignments, such as viewing diagrams and graphs in textbooks illustrating the various shapes of graphs such as those of exponential, logarithmic, polynomial or rational functions.
2. additional problem sets assigned as homework from the book, such as practice on finding roots and asymptotes of rational functions, or practice on determining all complex roots of a quadratic function.
3. graded assignments, such as problem sets on solving linear systems in two variables by elimination and substitution, or problem sets on determining all solutions to logarithmic equations and eliminating extraneous solutions.

## Articulation

C-ID Descriptor Number
MATH M150
Status
Aligned

## District General Education

## A. Natural Sciences

## B. Social and Behavioral Sciences

## C. Humanities

D. Language and Rationality

D2. Communication/Analytical Thinking
Approved
E. Health and Physical Education/Kinesiology
F. Ethnic Studies/Gender Studies

Course is CSU transferable
Yes
CSU Baccalaureate List effective term:
FALL 2020

## CSU GE-Breadth

## Area A: English Language Communication and Critical Thinking

## Area B: Scientific Inquiry and Quantitative Reasoning

B4 Mathematical/Quantitative Reasoning
Approved
Proposed
Date Proposed:
2/27/2019

## Area C: Arts and Humanities

Area D: Social Sciences

## Area E: Lifelong Learning and Self-Development

## CSU Graduation Requirement in U.S. History, Constitution and American Ideals: <br> UC TCA

UC TCA
Approved

Date Proposed:
6/5/2019

## IGETC

## Area 1: English Communication

## Area 1A: English Composition

Proposed
Date Proposed:
12/15/2019
Area 2A: Mathematical Concepts \& Quantitative Reasoning
Area 2A: Mathematical Concepts \& Quantitative Reasoning
Proposed

## Area 3: Arts and Humanities

Area 4: Social and Behavioral Sciences
Area 5: Physical and Biological Sciences
Area 6: Languages Other than English (LOTE)
Textbooks and Lab Manuals
Resource Type
Textbook
Description
Young, Cynthia Y. College Algebra. 4th ed. Wiley, 2017.

## Resource Type

Textbook
Description
Larson, Ron. College Algebra. 10th ed. Cengage, 2018.

## Resource Type

Textbook
Description
Lial, Margaret L. Essentials of College Algebra. 12th ed. Pearson, 2018.

## Resource Type

Textbook

## Description

Bittinger, Marvin L. College Algebra Graphs and Models. 6th ed. Pearson, 2016.

## Library Resources

Assignments requiring library resources
Use of textbooks on reserve.
Use of the Library's print and online resources to supplement application problems by researching models in various liberal arts studies, such as business, economics, biology, sociology and statistical studies related to these fields. Such applications may apply
to the analyzing of graphs, or the use of applied formulas requiring solving by analyzing polynomials, exponential, or logarithmic functions.

## Sufficient Library Resources exist

Yes

## Example of Assignments Requiring Library Resources

Using library resources to explore applications of functions and graphing, such as finding examples of structures or natural phenomena that simulate various graphs and shapes, including using measurements to compute heights, widths, areas and volumes.

## Distance Education Addendum

## Definitions

## Distance Education Modalities

Hybrid (51-99\% online)
Hybrid (1-50\% online)
100\% Online

## Faculty Certifications

Faculty assigned to teach Hybrid or Fully Online sections of this course will receive training in how to satisfy the Federal and state regulations governing regular effective/substantive contact for distance education. The training will include common elements in the district-supported learning management system (LMS), online teaching methods, regular effective/substantive contact, and best practices.
Yes
Faculty assigned to teach Hybrid or Fully Online sections of this course will meet with the EAC Alternate Media Specialist to ensure that the course content meets the required Federal and state accessibility standards for access by students with disabilities. Common areas for discussion include accessibility of PDF files, images, captioning of videos, Power Point presentations, math and scientific notation, and ensuring the use of style mark-up in Word documents.
Yes
Regular Effective/Substantive Contact
Hybrid (1\%-50\% online) Modality:

| Method of Instruction | Document typical activities or assignments for each method of <br> instruction |
| :--- | :--- |
| Asynchronous Dialog (e.g., discussion board) | Use of student discussion boards to discuss concepts from the material, <br> solutions to homework problems, general discussion of techniques in <br> solving problems, study skills, or arranging study groups. |
| E-mail | Responding to student queries about material, grade information, <br> course policies and procedures, scheduling and due dates, submitting <br> homework assignments, or making general announcements to the class. |
| Face to Face (by student request; cannot be required) | Students requesting to speak to instructor in person for personal help on <br> material, grade information, or discussion of policies and procedures. |
| Other DE (e.g., recorded lectures) | Posting of recorded lectures either by the instructor, recorded lessons <br> available through campus resources, or use of public online resources <br> available on the internet. |
| Synchronous Dialog (e.g., online chat) | Active live discussion with the instructor on material concepts, <br> techniques for problem solving, feedback on solutions to problems, <br> general chat on study skills, or answers to homework problems, quizzes <br> or tests. |

Hybrid (51\%-99\% online) Modality:

| Method of Instruction | Document typical activities or assignments for each method of <br> instruction |
| :--- | :--- |
| Asynchronous Dialog (e.g., discussion board) | Use of student discussion boards to discuss concepts from the material, <br> solutions to homework problems, general discussion of techniques in |
| solving problems, study skills, or arranging study groups. |  |


| E-mail | Responding to student queries about material, grade information, course policies and procedures, scheduling and due dates, submitting homework assignments, or making general announcements to the class. |
| :---: | :---: |
| Face to Face (by student request; cannot be required) | Students requesting to speak to instructor in person for personal help on material, grade information, or discussion of policies and procedures. |
| Other DE (e.g., recorded lectures) | Posting of recorded lectures either by the instructor, recorded lessons available through campus resources, or use of public online resources available on the internet. |
| Synchronous Dialog (e.g., online chat) | Active live discussion with the instructor on material concepts, techniques for problem solving, feedback on solutions to problems, general chat on study skills, or answers to homework problems, quizzes or tests. |
| 100\% online Modality: |  |
| Method of Instruction | Document typical activities or assignments for each method of instruction |
| Asynchronous Dialog (e.g., discussion board) | Use of student discussion boards to discuss concepts from the material, solutions to homework problems, general discussion of techniques in solving problems, study skills, or arranging study groups. |
| E-mail | Responding to student queries about material, grade information, course policies and procedures, scheduling and due dates, submitting homework assignments, or making general announcements to the class. |
| Other DE (e.g., recorded lectures) | Posting of recorded lectures either by the instructor, recorded lessons available through campus resources, or use of public online resources available on the internet. |
| Synchronous Dialog (e.g., online chat) | Active live discussion with the instructor on material concepts, techniques for problem solving, feedback on solutions to problems, general chat on study skills, or answers to homework problems, quizzes or tests. |

## Examinations

Hybrid (1\%-50\% online) Modality
On campus
Hybrid (51\%-99\% online) Modality
On campus

## Primary Minimum Qualification

MATHEMATICS

## Review and Approval Dates

## Department Chair

M01/08/2019

## Dean

01/08/2019

## Technical Review

01/31/2019

## Curriculum Committee

02/05/2019
DTRW-I
09/12/2019

## Curriculum Committee

MM/DD/YYYY

## Board

10/08/2019
CCCCO
10/12/2019
Control Number CCC000608544

DOE/accreditation approval date
MM/DD/YYYY

