Module 4 – Conversion Factors

Prerequisite
Module 4 requires Lessons 1A and 1B (on exponential fundamentals) and 2A and 2B (on metric fundamentals). Lesson 2C and Module 3 will be helpful, but not essential, for most of the problems in Module 4.

If you are in a hurry to catch up in order to begin conversion factors, you may return to the other lessons in Modules 1-3 at a later time. (The other lessons in Modules 1-3 will be needed for later modules.)

* * * * *

Introduction
The material in Module 4 may be a review of what you have learned previously. Each lesson will include suggestions for how you can complete this review quickly.

However, some rules in Module 4 that you may not know, such as “writing the wanted unit first,” and using the “starting template.” These rules will be important in solving complex problems in later lessons. Be sure to read each section and do at least the last two problems in each practice set.

* * * * *

Lesson 4A: Conversion Factor Basics

Conversion factors can be used to change from one unit of measure to another, or to find measures of substances or processes that are equivalent.

A conversion factors is a fraction that equals one. Multiplying a quantity by a conversion factor changes the units that measure a quantity but does not change the original amount of the quantity.

Conversion factors equal unity (1) because they are made from equalities. For any fraction in which the top and bottom are equal, its value is one.

For example: \( \frac{7}{7} = 1 \)

Or, since 1000 milliliters = 1 liter; \( \frac{1000 \text{ mL}}{1 \text{ liter}} = 1 \), and \( \frac{1 \text{ liter}}{1000 \text{ mL}} = 1 \)

These last two fractions are typical conversion factors. Any fraction that equals one right-side up will also equal one up-side down. Any conversion factor can be inverted (flipped over) for use if necessary, and it will still be equal to one.

“Conversion factor” is a term for a ratio, or fraction, or two measured quantities that are equal or equivalent in a problem. Our method of solving problems will focus on finding equal or equivalent quantities. We will use those equalities to construct conversion factors.
Let’s try an example of conversion-factor math. Try the following problem. Show your work on the page or in your problem notebook, then check your answer below.

Multiply \(0.75 \text{ kilometers} \times \frac{1000 \text{ meters}}{1 \text{ kilometer}}\) = \(1 \text{ kilometer}\)

* * * * * ( * * * mean: cover below, write your answer, then check below.)

**Answer**

\[0.75 \text{ kilometers} \times \frac{1000 \text{ meters}}{1 \text{ kilometer}} = (0.75 \times 1000) \text{ meters} = 750 \text{ meters}\]

When these terms are multiplied, the “like units” on the top and bottom cancel, leaving meters as the unit on top.

Since the conversion factor multiplies the given quantity by one, the answer equals the given amount that we started with. This answer means that 750 meters is the same as 0.75 km.

Multiplying by conversion factors changed the unit, but not the amount, of the given quantity. The result is what we started with, measured in different units.

This process answers a question posed in many science problems: From the units we are given, how can we obtain the units we want?

* * * * *

**Summary**

- Conversion factors are made from ratios, fractions, or two measured quantities that are equivalent, related, or equal in a problem.
- Conversion factors equal one, because the top and bottom terms are equal or equivalent.
- When the units cancel correctly and the numbers are where they should be to make legal conversion factors, the answer will be a correct conversion from the starting given units to the final wanted units.

⇒ Units tell you where to place the numbers to solve a calculation correctly.

* * * * *
**Practice:** Try every other lettered problem. Check your answers frequently. If you miss one on a section, try a few more. Answers are on the next page.

1. Multiply the conversion factors. Cancel units that cancel, then group the numbers and do the math. Write the answer number and unit.

   a. \[225 \text{ centigrams} \cdot \frac{1 \text{ gram}}{100 \text{ centigrams}} \cdot \frac{1 \text{ kilogram}}{1000 \text{ grams}} = \]

   = \[100 \text{ centigrams} \]

   b. \[1.5 \text{ hours} \cdot \frac{60 \text{ minutes}}{1 \text{ hour}} \cdot \frac{60 \text{ seconds}}{1 \text{ minute}} = \]

   = \[1 \text{ hour} \]

2. To be legal, the top and bottom of conversion factors must be equal. Label these conversion factors as legal or illegal.

   a. \[1000 \text{ mL} \]

   = \[1 \text{ liter} \]

   b. \[1000 \text{ liters} \]

   = \[1 \text{ milliliter} \]

   c. \[1.00 \text{ g H}_2\text{O} \]

   = \[1 \text{ mL H}_2\text{O} \]

   d. \[1 \text{ volt} \]

   = \[100 \text{ centivolts} \]

   e. \[1 \text{ mL} \]

   = \[1 \text{ cc} \]

   f. \[10^3 \text{ cm}^3 \]

   = \[1 \text{ L} \]

   g. \[1000 \text{ kilowatts} \]

   = \[1 \text{ watt} \]

   h. \[1 \text{ kilocalorie} \]

   = \[10^3 \text{ calories} \]

3. Add numbers to make legal conversion factors, with at least one of the numbers in each conversion factor being a 1.

   a. \[\quad \frac{\text{grams}}{\text{kilograms}} \]

   b. \[\quad \frac{\text{mole}}{\text{nаномоль}} \]

   c. \[\quad \frac{\text{cm}^3}{\text{мл}} \]

   d. \[\quad \frac{\text{centijoules}}{\text{joules}} \]

   e. \[\quad \frac{\text{liters}}{\text{кубический сантиметр}} \]

   f. \[\quad \frac{\text{curie}}{\text{пикокюри}} \]

4. Finish these.

   a. \[27 \text{A} \cdot \frac{2 \text{T}}{8 \text{A}} \cdot \frac{4 \text{W}}{3 \text{T}} = \]

   b. \[2.5 \text{ meters} \cdot \frac{10^2 \text{ cm}}{1 \text{ meter}} = \]

   c. \[33 \text{ grams} \cdot \frac{1 \text{ kilogram}}{10^3 \text{ grams}} = \]

   d. \[95 \text{ km} \cdot \frac{0.625 \text{ miles}}{1 \text{ km}} = \]

   e. \[27 \text{ meters} \cdot \frac{60 \text{ s}}{1 \text{ min}} \cdot \frac{60 \text{ min}}{1 \text{ hour}} \cdot \frac{1 \text{ kilometer}}{10^3 \text{ meters}} = \]

   * * * * *
ANSWERS

1. a. \(225 \text{ centigrams} \cdot \frac{1 \text{ gram}}{100 \text{ centigrams}} \cdot \frac{1 \text{ kilogram}}{1000 \text{ grams}} = 225 \times \frac{1}{10} \times \frac{1}{1000} \text{ kg} = 0.00225 \text{ kilograms}\)

   The answer means that 0.00225 kg is equal to 225 cg.

   b. \(1.5 \text{ hours} \cdot \frac{60 \text{ minutes}}{1 \text{ hour}} \cdot \frac{60 \text{ seconds}}{1 \text{ minute}} = 1.5 \times 60 \times 60 \text{ s} = 5400 \text{ s} \quad \text{or} \quad 5.4 \times 10^3 \text{ s}\)

   Recall that s is the SI abbreviation for seconds. This answer means that 1.5 hours is equal to 5,400 seconds.

2. a. \(\frac{1000 \text{ mL}}{1 \text{ liter}}\)
   b. \(\frac{1000 \text{ liters}}{1 \text{ milliliter}}\)
   c. \(\frac{1.00 \text{ g H}_2\text{O}}{1 \text{ mL H}_2\text{O}}\)
   d. \(\frac{1 \text{ volt}}{100 \text{ centivolts}}\)

   [Legal] [Illegal] [Legal if liquid water] [Legal]

   e. \(\frac{1 \text{ mL}}{1 \text{ cc}}\)
   f. \(\frac{10^3 \text{ cm}^3}{1 \text{ L}}\)
   g. \(\frac{1000 \text{ kilowatts}}{1 \text{ watt}}\)
   h. \(\frac{1 \text{ kilocalorie}}{10^3 \text{ calories}}\)

   [Legal] [Legal] [Illegal] [Legal]

3. a. \(\frac{1000 \text{ grams}}{1 \text{ kilogram}}\) or \(\frac{1 \text{ gram}}{10^3 \text{ kilogram}}\)
   b. \(\frac{1 \text{ mole}}{10^9 \text{ nanomole}}\) or \(\frac{10^9 \text{ nanomole}}{1 \text{ mole}}\)
   c. \(\frac{1 \text{ cm}^3}{1 \text{ mL}}\)
   d. \(\frac{100 \text{ centijoules}}{1 \text{ joule}}\) or \(\frac{1 \text{ joule}}{10^2 \text{ centijoules}}\)
   e. \(\frac{1000 \text{ cc}}{1 \text{ cubic cm}}\) or \(\frac{1 \text{ cubic cm}}{10^3 \text{ liters}}\)
   f. \(\frac{10^{-12} \text{ curie}}{1 \text{ curie}}\) or \(\frac{1 \text{ curie}}{10^{12} \text{ picocurie}}\)

4. a. \(\frac{27 \text{ A} \cdot 2\text{ T} \cdot 4\text{ W}}{8\text{ A} \cdot 3\text{ T} \cdot 8\text{ A}} = \frac{27 \cdot 2 \cdot 4 \cdot 3}{8 \cdot 3} \text{ W} = 9\text{ W}\)
   b. \(2.5 \text{ meters} \cdot \frac{10^2 \text{ cm}}{1 \text{ meter}} = 2.5 \times 10^2 = 250 \text{ cm}\)
   c. \(\frac{33 \text{ grams}}{1 \text{ kilogram}} = \frac{33}{10^3} = 0.033 \text{ kg}\)
   d. \(\frac{95 \text{ km}}{1 \text{ km}} \cdot \frac{0.625 \text{ miles}}{1 \text{ hour}} = 95 \cdot 0.625 = 59 \text{ miles}\)
   e. \(\frac{27 \text{ meters}}{1 \text{ min}} \cdot \frac{60 \text{ s}}{1 \text{ hour}} \cdot \frac{1 \text{ kilometer}}{10^3 \text{ meters}} = \frac{27 \cdot 60 \cdot 60}{10^3 \text{ hour}} = 97 \text{ km}\)

* * * * *
Lesson 4B: Single Step Conversions

In the previous lesson, conversion factors were supplied. In this lesson, you will learn to make your own conversion factors to solve problems.

Let’s use this simple word problem as an example.

Q. How many years is 925 days?

In your notebook, write an answer to each step below.

Steps for Solving with Conversion Factors

1. Begin by writing a question mark (?) and then the unit you are looking for in the problem, the answer unit.

2. Next write an equal sign. It means, “OK, that part of the problem is done. From here on, leave the answer unit alone.” You don’t cancel the answer unit, and you don’t multiply by it.

3. After the = sign, write the number and unit you are given (the known quantity).

At this point, in your notebook should be ? years = 925 days

4. Next, write a • and a line _______ for a conversion factor to multiply by.

5. A key step: write the unit of the given quantity in the denominator (on the bottom) of the conversion factor. Leave room for a number in front.

   Do not put the given number in the conversion – just the given unit.

   ? years = 925 days • __________
   days

6. Next, write the answer unit on the top of the conversion factor.

   ? years = 925 days • ______ year
   days

7. Add numbers that make the numerator and denominator of the conversion factor equal. In a legal conversion factor, the top and bottom quantities must be equal or equivalent.

8. Cancel the units that you set up to cancel.

9. If the unit on the right side after cancellation is the answer unit, stop adding conversions. Write an = sign. Multiply the given quantity by the conversion factor. Write the number and the un-canceled unit. Done!

Finish the above steps, then check your answer below.

*   *   *   *   *

? years = 925 days • \( \frac{1 \text{ year}}{365 \text{ days}} \) = \( \frac{925 \text{ years}}{365} \) = 2.53 years

(Sig figs: 1 is exact, 925 has 3 sf, 365 has 3 sf (1 yr. = 365.24 days), round to 3 sf.)
You may need to look back at the above steps on occasion, but you should not need to memorize them. By doing the following problems, you will quickly learn what you need to know.

* * * * *

**Practice:** After each numbered problem, check your answers at the end of this lesson. Look back at the steps if needed.

In the problems in this practice section, write conversions in which one of the numbers (in the numerator or the denominator) is a 1.

If these are easy, do every second or third letter. If you miss a few, do a few more.

1. Add numbers to make these conversion factors legal, cancel the units that cancel, multiply the given by the conversion, and write your answer.

   a. \[? \text{ cm} = 0.35 \text{ meters} \cdot \frac{\text{cm}}{1 \text{ meter}} = \]
   b. \[? \text{ days} = 96 \text{ hours} \cdot \frac{\text{day}}{24 \text{ hours}} = \]
   c. \[? \text{ mL} = 3.50 \text{ liters} \cdot \frac{\text{mL}}{1 \text{ liter}} = \]
   d. \[? \text{ minutes} = 330 \text{ s} \cdot \frac{\text{minutes}}{\text{seconds}} = \]

2. To start these, put the unit of the given quantity where it will cancel. Then finish the conversion factor, do the math, and write your answer with its unit.

   a. \[? \text{ seconds} = 0.25 \text{ minutes} \cdot \frac{\text{sec.}}{1} = \]
   b. \[? \text{ kilograms} = 250 \text{ grams} \cdot \frac{\text{kilogram}}{10^3} = \]
   c. \[? \text{ meters} = 14 \text{ cm} \cdot \frac{\text{cm}}{\text{cm}} = \]
   d. \[? \text{ days} = 2.73 \text{ years} \cdot \frac{365}{\text{days}} = \]
   e. \[? \text{ years} = 200. \text{ days} \cdot \frac{1}{\text{days}} = \]
3. You should not need to memorize the written rules for arranging conversion factors; the steps will quickly become automatic with practice. However, it is helpful to memorize this “single unit starting template.”

When solving for single units, begin with

\[ \text{? unit WANTED} = \text{number and UNIT given \cdot \frac{\text{UNIT given}}{}} \]

The template emphasizes that your first conversion factor puts the given unit (but not the given number) where it will cancel.

a. \( \text{? months} = 5.0 \text{ years \cdot \frac{?}{}} \)

b. \( \text{? liters} = 350 \text{ milliliters \cdot \frac{?}{}} \)

c. \( \text{? minutes} = 5.5 \text{ hours \cdot \frac{?}{}} \)

4. Use the starting template to find how many hours equal 390 minutes.

5. \( \text{? milligrams} = 0.85 \text{ kg \cdot \frac{? \text{ gram}}{\text{kg}} \cdot \frac{?}{\text{gram}}} \)

* * * * *

**ANSWERS**

Some but not all unit cancellations are shown. For your answer to be correct, it must include its unit. Your conversions may be in different formats, such as \( 1 \text{ kg} = 1,000 \text{ g} \) or \( 1 \text{ g} = 10^{-3} \text{ kg} \), as long as the top and bottom are equal and you get the same answers as below.

1. a. \( \text{? cm} = 0.35 \text{ meters \cdot \frac{100 \text{ cm}}{1 \text{ meter}}} = 0.35 \cdot 100 = 35 \text{ cm} \)

(Sig figs: 0.35 has 2 sf, prefix definitions are exact with infinite sf, answer is rounded to 2 sf)

b. \( \text{? days} = 96 \text{ hours \cdot \frac{1 \text{ day}}{24 \text{ hours}}} = 96 \cdot \frac{1}{24} = 4.0 \text{ days} \)
Lesson 4C: Multi-Step Conversions

In Problem 5 at the end of the previous lesson, we did not know a direct conversion from kilograms to milligrams. However, we knew a conversion from kilograms to grams, and another from grams to milligrams.

In most problems, you will not know a single conversion from the given to wanted unit, but there will be known conversions that you can chain together to solve.
Solving With Multiple Conversions

If the unit on the right after you cancel units is not the answer unit, get rid of it. Write it in the next conversion factor where it will cancel.

Finish the next conversion with a known conversion, one that either includes the answer unit, or gets you closer to the answer unit.

In making conversions, set up units to cancel, but add numbers that make legal conversions.

* * * * *

Practice

Write the six metric fundamentals from memory. Use those fundamentals for the problems below.

These are in pairs. If Part A is easy, go to Part A of the next question. If you need help with Part A, do Part B for more practice.

1. a. ? kilograms = 760 milligrams • gram • ____________ =

   b. ? cg = 4.2 kg • __________ • __________ =

2. a. ? years = 2.63 x 10^4 hours • __________ • __________ =

   b. ? seconds = 1.00 days • hr • ________ • ________ =

3. a. ? mg H_2O(l) = 1.5 cc H_2O(l) • g H_2O(l) • __________ =

   b. ? kg H_2O(liquid) = 5.5 liter H_2O(l) • __________ • __________ • ________ =

* * * * *

Answers

For visibility, not all cancellations are shown, but cancellations should be marked on your paper.

1a. ? kilograms = 760 milligrams • \( \frac{1 \text{ g}}{10^3 \text{ mg}} \) • \( \frac{1 \text{ kg}}{10^3 \text{ g}} \) = \( 7.6 \times 10^{-4} \text{ kg} \)

   b. ? cg = 4.2 kg • \( \frac{10^3 \text{ g}}{1 \text{ kg}} \) • \( \frac{10^2 \text{ cg}}{1 \text{ g}} \) = \( 4.2 \times 10^5 \text{ cg} \)
2a. \[ ? \text{ years} = 2.63 \times 10^4 \text{ hours} \]
\[ \frac{1 \text{ day}}{24 \text{ hr}} \cdot \frac{1 \text{ yr}}{365 \text{ days}} = \frac{2.63 \times 10^4}{24 \cdot 365} = 3.00 \text{ years} \]

b. \[ ? \text{ seconds} = 1.00 \text{ days} \]
\[ \frac{24 \text{ hr}}{1 \text{ day}} \cdot \frac{60 \text{ min}}{1 \text{ hr}} \cdot \frac{60 \text{ sec}}{1 \text{ min}} = 8.64 \times 10^4 \text{ sec.} \]

3a. \[ ? \text{ mg} \text{ H}_2\text{O}(l) = 1.5 \text{ cc} \text{ H}_2\text{O}(l) \]
\[ \frac{1 \text{ g} \text{ H}_2\text{O}(l)}{1 \text{ cc} \text{ H}_2\text{O}(l)} \cdot \frac{10^3 \text{ mg}}{1 \text{ g}} = 1.5 \times 10^3 \text{ mg} \text{ H}_2\text{O}(l) \]

b. \[ ? \text{ kg} \text{ H}_2\text{O}(l) = 5.5 \text{ liter} \text{ H}_2\text{O}(l) \]
\[ \frac{4000 \text{ mL}}{1 \text{ L}} \cdot \frac{1.00 \text{ g} \text{ H}_2\text{O}(l)}{1 \text{ mL} \text{ H}_2\text{O}(l)} \cdot \frac{1 \text{ kg}}{10^3 \text{ g}} = 5.5 \text{ kg} \text{ H}_2\text{O}(l) \]

* * * * *

Lesson 4D: English/Metric Conversions

Using Familiar Conversions
All of the unit conversions between units that we have used so far have had the number 1 on either the top or the bottom, but a one is not required in a legal conversion.

Both “1 kilometer = 1,000 meters” and “3 kilometers = 3,000 meters” are true equalities, and both equalities could be used to make legal conversion factors. In most cases, however, conversions with a 1 are preferred.

Why? We want conversions to be familiar and easy to remember, so that we can write them automatically, and quickly check that they are correct. Definitions are usually based on one of a unit, such as “1 km = 1,000 meters.” Definitions are the most frequently encountered conversions, and are therefore the most familiar.

Other conversions may be familiar even if they do not include a 1. For example, many cans of soft drinks are labeled “12.0 fluid ounces (355 mL).” This supplies an equality for English-to-metric volume units: 12.0 fluid ounces = 355 mL. That is a legal conversion and, because its numbers and units are seen often, it is a good conversion to use because it is easy to remember.

Bridge Conversions

Science problems often involve a key bridge conversion between one unit system, or one substance, and another.

For example, a bridge conversion between the metric and English-system distance units is

\[
2.54 \text{ centimeters} = 1 \text{ inch}
\]

Using this equality, we can convert back and forth between metric and English measurements of distance.

Any metric-English distance equality can be used to convert between distance measurements in the two systems. \[ 1 \text{ mile} = 1.61 \text{ km} \] is another metric-English conversion for distance that is frequently used. However, in our initial practice in these lessons, the cm-to-inch conversion will be the one used most often.
In problems that require bridge conversions, our strategy to begin will be to “head for the bridge,” to begin by converting to one of the two units in the bridge conversion.

When a problem needs a bridge conversion, use these steps.

1) First convert the given unit to the one of the two bridge units that is in the same system as the given quantity.

2) Next, multiply by the bridge conversion. The bridge conversion crosses over from the given system into the WANTED system of the answer.

3) Multiply by other conversions in the WANTED system to get the final answer unit.

Conversions between the metric and English measurement systems provide a way to practice the bridge-conversion methods we will use in chemical reaction calculations.

Add these English distance-unit definitions to your list of memorized conversions.

\[
12 \text{ inches} = 1 \text{ foot} \quad 3 \text{ feet} = 1 \text{ yard} \quad 5,280 \text{ feet} = 1 \text{ mile}
\]

Memorize and use this metric to English bridge conversion for distance.

\[
2.54 \text{ centimeters} = 1 \text{ inch}
\]

Then cover the answer below and apply the steps and conversions above to this problem.

**Q.** \( \text{? feet} = 1.00 \text{ meter} \)

**Answer**

Since the wanted unit is English, and the given unit is metric, an English/metric bridge is needed.

**Step 1:** Head for the bridge. Since the given unit (meters) is metric system, convert to the metric unit used in the bridge conversion (2.54 cm = 1 inch) -- centimeters.

\[
\text{? feet} = 1.00 \text{ meter} \times \frac{100 \text{ cm}}{1 \text{ meter}} \times \frac{1 \text{ inch}}{2.54 \text{ cm}}
\]

Note the start of the next conversion. Since cm is not the wanted answer unit, cm must be put in the next conversion where it will cancel. If you start the “next unit to cancel” conversion automatically after finishing the prior conversion, it helps to arrange and choose the next conversion.

Adjust and complete your work if needed.

**Step 2:** Complete the bridge that converts to the system of the answer: English units.

\[
\text{? feet} = 1.00 \text{ meter} \times \frac{100 \text{ cm}}{1 \text{ meter}} \times \frac{1 \text{ inch}}{2.54 \text{ cm}} \times \frac{1 \text{ inch}}{1 \text{ inch}}
\]
Step 3: Get rid of the unit you’ve got. Get the unit you want.

\[
? \text{ feet} = 1.00 \text{ meter} \cdot \frac{100 \text{ cm}}{1 \text{ meter}} \cdot \frac{1 \text{ inch}}{2.54 \text{ cm}} \cdot \frac{1 \text{ foot}}{12 \text{ inches}} = 3.28 \text{ feet}
\]

The answer tells us that 1.00 meter (the given quantity) is equal to 3.28 feet.

Some science problems take 10 or more conversions to solve. However, if you know that a
bridge conversion is needed, “heading for the bridge” breaks the problem into pieces.
Solving in pieces will simplify your navigation to the answer.

* * * * *

Practice: Use the bridge conversion above. Start by doing every other problem. Do
more if you need more practice.

1. \(? \text{ cm} = 12.0 \text{ inches} \cdot \text{__________} = \)

2. \(? \text{ inches} = 1.00 \text{ meters} \cdot \text{__________} \cdot \text{__________} \)

3. For \(? \text{ inches} = 760. \text{ mm} \)
   a. To what unit to you aim to convert the given in the initial conversions? Why?
   b. Solve: \(? \text{ inches} = 760. \text{ mm} \)

4. \(? \text{ mm} = 0.500 \text{ yards} \)

5. For \(? \text{ km} = 1.00 \text{ mile} \), to convert using 1 inch = 2.54 cm,
   a. To what unit to you aim to convert the given in the initial conversions? Why?
   b. Solve: \(? \text{ km} = 1.00 \text{ mile} \)

6. Use as a bridge conversion for mass units, 1 kilogram = 2.2 lbs.
   \(? \text{ grams} = 7.7 \text{ lbs} \)

7. Use the “soda can” volume conversion (12.0 fluid ounces = 355 mL).
   \(? \text{ fluid ounces} = 2.00 \text{ liters} \)

* * * * *
ANSWERS

In these answers, some but not all of the unit cancellations are shown. The definition 1 cm = 10 mm may be used for mm to cm conversions. Doing so will change the number of conversions but not the answer.

1. \( ? \text{ cm} = 12.0 \text{ inches} \times \frac{2.54 \text{ cm}}{1 \text{ inch}} = 12.0 \times 2.54 = 30.5 \text{ cm} \) (check the cm on a 12 inch ruler)

2. \( ? \text{ inches} = 1.00 \text{ meters} \times \frac{100 \text{ cm}}{1 \text{ meter}} \times \frac{1 \text{ inch}}{2.54 \text{ cm}} = 100 \times \frac{1}{2.54} = 39.4 \text{ inches} \)

3a. Aim to convert the given unit (mm) to the bridge unit that is in the same system (English or metric) as the given. Cm is the bridge unit in the same system as mm.

3b. \( ? \text{ inches} = 760. \text{ mm} \times \frac{1 \text{ meter}}{1000 \text{ mm}} \times \frac{1 \text{ inch}}{2.54 \text{ cm}} \times \frac{1 \text{ meter}}{1 \text{ inch}} = \frac{760}{10 \times 2.54} = 29.9 \text{ inches} \)

Sig figs: 760., with the decimal after the 0, means 3 sig figs. Metric definitions and 1 have infinite sig figs. The answer must be rounded to 3 sig figs (see Module 2).

In countries that use English units for legal measure, 1 inch = 2.54 cm is now the definition of an inch. However, unless an equality is termed exact or a definition, you should assume that in conversions and equalities, a 1 is exact, but other numbers are precise only to the sig figs shown.

4. \( ? \text{ mm} = 0.500 \text{ yd} \times \frac{3 \text{ ft}}{1 \text{ yd}} \times \frac{12 \text{ in}}{1 \text{ ft}} \times \frac{2.54 \text{ cm}}{1 \text{ inch}} \times \frac{1 \text{ meter}}{100 \text{ cm}} \times \frac{1000 \text{ mm}}{1 \text{ meter}} = 457 \text{ mm} \)

5a. Aim to convert the given unit (miles) to the bridge unit in the same system (English or metric) as the given. Inches is in the same system as miles.

5b. \( ? \text{ km} = 1 \text{ mile} \times \frac{5280 \text{ ft}}{1 \text{ mile}} \times \frac{12 \text{ in}}{1 \text{ ft}} \times \frac{2.54 \text{ cm}}{1 \text{ inch}} \times \frac{1 \text{ meter}}{100 \text{ cm}} \times \frac{1 \text{ km}}{1000 \text{ meter}} = 1.61 \text{ km} \)

Sig figs: Assume an integer 1 that is part of an equality or conversion is exact, with infinite sig figs.

6. \( ? \text{ grams} = 7.7 \text{ lbs} \times \frac{1 \text{ kg}}{2.2 \text{ lb}} \times \frac{10^3 \text{ grams}}{1 \text{ kg}} = 3.5 \times 10^3 \text{ grams} \)

Sig figs: 7.7 and 2.2 have 2 sig figs. A 1 has infinite sig figs. Definitions, including metric-prefix definitions, have infinite sig figs. Round the answer to 2 sig figs.

7. \( ? \text{ fluid ounces} = 2.00 \text{ liters} \times \frac{1000 \text{ mL}}{1 \text{ liter}} \times \frac{12.0 \text{ fl. oz.}}{355 \text{ mL}} = 67.6 \text{ fl. oz.} \)

(Check this answer on any 2-liter soda bottle.)